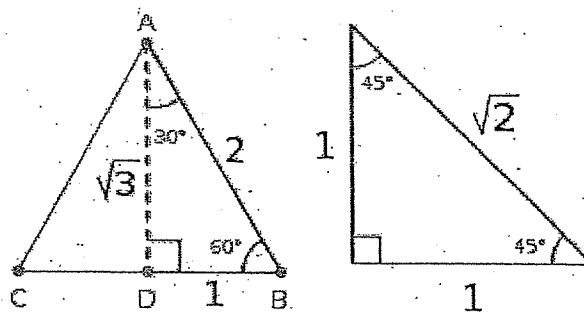


## Special Triangles and Triangle Formulas

Degrees	Radians	sin	cos	tan
0	0	0	1	0
30	$\pi/6$	$1/2$	$\sqrt{3}/2$	$\sqrt{3}/3$
45	$\pi/4$	$\sqrt{2}/2$	$\sqrt{2}/2$	1
60	$\pi/3$	$\sqrt{3}/2$	$1/2$	$\sqrt{3}$
90	$\pi/2$	1	0	-



Function	Abbreviation	Description	Identities (using radians)
Sine	sin	$\frac{\text{opposite}}{\text{hypotenuse}}$	$\sin \theta \equiv \cos \left( \frac{\pi}{2} - \theta \right) \equiv \frac{1}{\csc \theta}$
Cosine	cos	$\frac{\text{adjacent}}{\text{hypotenuse}}$	$\cos \theta \equiv \sin \left( \frac{\pi}{2} - \theta \right) \equiv \frac{1}{\sec \theta}$
Tangent	tan (or tg)	$\frac{\text{opposite}}{\text{adjacent}}$	$\tan \theta \equiv \frac{\sin \theta}{\cos \theta} \equiv \cot \left( \frac{\pi}{2} - \theta \right) \equiv \frac{1}{\cot \theta}$
Cotangent	cot (or ctg or ctr)	$\frac{\text{adjacent}}{\text{opposite}}$	$\cot \theta \equiv \frac{\cos \theta}{\sin \theta} \equiv \tan \left( \frac{\pi}{2} - \theta \right) \equiv \frac{1}{\tan \theta}$
Secant	sec	$\frac{\text{hypotenuse}}{\text{adjacent}}$	$\sec \theta \equiv \csc \left( \frac{\pi}{2} - \theta \right) \equiv \frac{1}{\cos \theta}$
Cosecant	csc (or cosec)	$\frac{\text{hypotenuse}}{\text{opposite}}$	$\csc \theta \equiv \sec \left( \frac{\pi}{2} - \theta \right) \equiv \frac{1}{\sin \theta}$

REMEMBER

THEN

TO DERIVE

$$\sin^2 \theta + \cos^2 \theta = 1$$

Divide by  $\cos^2 \theta$   
Divide by  $\sin^2 \theta$

$$\tan^2 \theta + 1 = \sec^2 \theta$$

$$1 + \cot^2 \theta = \csc^2 \theta$$

$$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

Substitute A for B(+)

$$\sin(2A) = 2 \sin A \cos A$$

$$\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

Use A-B, let B=(-A)

$$\cos(2A) = \cos^2 A - \sin^2 A$$

$$= 1 - 2 \sin^2 A$$

$$= 2 \cos^2 A - 1$$

$$\sin^2 \theta = \frac{1 - \cos(2\theta)}{2}$$

$$\sin \theta = \pm \sqrt{\frac{1 - \cos 2\theta}{2}}$$

$$\sin \frac{\theta}{2} = \pm \sqrt{\frac{1 - \cos \theta}{2}}$$

$$\cos^2 \theta = \frac{1 + \cos(2\theta)}{2}$$

$$\cos \theta = \pm \sqrt{\frac{1 + \cos 2\theta}{2}}$$

$$\cos \frac{\theta}{2} = \pm \sqrt{\frac{1 + \cos \theta}{2}}$$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

Therefore,  $\tan^2 \theta = \frac{\sin^2 \theta}{\cos^2 \theta}$

## Geometry formulas

	Line Midpoint
$M = \left( \frac{x_1+x_2}{2}, \frac{y_1+y_2}{2} \right)$	Line Slope
$m = \frac{y_2-y_1}{x_2-x_1}$	Distance Formula
$d = \frac{\sqrt{(x_2-x_1)^2 + (y_2-y_1)^2}}{2}$	Slope-Intercept Form
$y = mx + b$	Point-Slope Form
$y - y_1 = m(x - x_1)$	Arc
$A = \frac{1}{2}r^2\theta$	Circle
$A = \pi r^2$	Triangle
$A = \frac{1}{2}bh$	Right Triangle
$A = \frac{1}{2}ab$	Isosceles Triangle
$A = \frac{\sqrt{3}}{4}a^2$	Square
$P = 4s$	Rectangle
$P = 2a + 2b$	Parallelogram
$P = 2a + 2b$	Trapezoid
$P = a + b + c + d$	Regular n-gon
$P = ns$	Right Regular Prism
$S = 2(ab + ac + bc)$	Cube
$S = 6s^2$	Right Prism
$S = 2A + Ph$	Right Regular Pyramid
$S = A + \frac{1}{2}Cl$	Rt. Circular Cylinder
$S = 2A + Ch = 2\pi r^2 + 2\pi rh$	Rt. Circular Cone
$S = A + \frac{1}{2}Cl$	Sphere
$S = 4\pi r^2$	Angle Sum of a Polygon
$= 180(n - 2)$	Heron's formula:
$A = \sqrt{s(s-a)(s-b)(s-c)}$ where $s = \frac{a+b+c}{2}$	Euler's formula:
$Faces + Vertices = Edges + 2$	